

Compound Interest

Type-I

To Find CI when Interest is Compound Annually.

Q.1 Find the amount and the CI on ₹ 250 for 2 years at 10% per annum.

Sol:-

Given that

$$\text{Principal} = ₹ 2500$$

$$\text{Time} = 2 \text{ years}$$

$$\text{Rate} = 10\%$$

$$\text{Interest for the 1st year} = \frac{P \times R \times T}{100}$$

$$= \frac{2500 \times 10 \times 1}{100}$$

$$= 250$$

$$\begin{aligned} \text{Amount at the end of the 1st year} &= 2500 \\ &\quad + 250 \\ &= \underline{\underline{2750}} \end{aligned}$$

$$\begin{aligned} \text{Interest for 2nd year} &= \frac{2750 \times 10 \times 1}{100} \\ &= 275 \end{aligned}$$

$$\begin{aligned} \text{Amount at the end of second year} &= 2750 \\ &\quad + 275 \\ &= \underline{\underline{3025}} \end{aligned}$$

$$\begin{aligned} \text{Amount} &= ₹ 3025 & \text{CI} &= 250 \\ &&&+ 275 \\ &&&= \underline{\underline{525}} \end{aligned}$$

Type-II

To Find CI when Interest is compounded half-yearly.

Find the CI on ₹ 5000 for 1 year at 8% per annum, CI half-yearly

Rate of interest = 8% P.a. = 4% per half-year
Time = 1 year = 2 half-years

Original Principal = ₹ 5000

Interest for 1st year (half-year) = $\frac{5000 \times 4 \times 1}{100} = ₹ 200$

Amount at the end of the first half year

$$= (5000 + 200) = ₹ 5200$$

Principal for 2nd year = ₹ 5200

Interest for the 2nd year (half) = $\frac{5200 \times 4 \times 1}{100} = ₹ 208$

Amount at the end of 2nd half year = ₹ 5200 + ₹ 208

$$= 5000 + \frac{5200 \times 4 \times 1}{100} = ₹ 5408$$

$$CI = ₹ 5408 - ₹ 5000 = ₹ 408$$

in ₹ 5408 for 2nd case

The difference between the C.I. and S.I.
on a certain sum for 2 years at 15%
per annum is ₹ 180. Find the sum.

Given that

$$\text{Rate} = 15\%$$

$$\text{Time} = 2 \text{ years}$$

$$\text{difference between CI and SI} = 180$$

Let be the principal ₹ P

$$\text{S.I.} = \frac{P \times R \times T}{100}$$

$$= \frac{P \times 15 \times 2}{100}$$

$$\text{S.I.} = \frac{3P}{10}$$

According to Ques.

$$\Rightarrow \text{C.I.} - \text{S.I.} = 180$$

$$\text{C.I.} = A - P = P \left(1 + \frac{R}{100}\right)^n - P$$

$$\frac{129P}{400} - \frac{3P}{10} = 180$$

$$= P \left(1 + \frac{\frac{15}{100}}{20}\right)^2 - P$$

$$\Rightarrow \frac{9P}{400} = 180$$

$$= P \left(1 + \frac{3}{20}\right)^2 - P$$

$$\Rightarrow P = \frac{180 \times 400}{81}$$

$$\text{C.I.} = \frac{529P - 400P}{400}$$

$$\Rightarrow P = ₹ 8000$$

$$\text{C.I.} = \frac{129P}{400}$$

Hence, the required
sum is ₹ 8000. Ans

Q:- A scooter is bought at ₹ 56000. If its value depreciates at the rate of 10% per annum. what will be its value after 3 years?

Given that
Price of scooter = ₹ 56000
Rate = 10 % p.a.
Time = 3 years

$$\text{Depreciate value of Scooter} = P \left(1 - \frac{R}{100}\right)^n$$

$$= 56000 \left(1 - \frac{10}{100}\right)^3$$

$$= 56000 \left(\frac{10 - 1}{10}\right)^3$$

$$= 56000 \times \frac{9}{10} \times \frac{9}{10} \times \frac{9}{10}$$

$$= 56 \times 729$$

$$= ₹ 40824$$

Hence, the required depreciate value is ₹ 40824

₹ 40824 And —

Ques:- In a certain experiment the count of bacteria was increasing at the rate of 2.5% per hour. Initially, the count was 512000. Find the bacteria at the end of 2 hours.

Sol:-

Given that

Initially bacteria was count = 512000

Rate = 2.5% or $\frac{5}{2}\%$

time = 2 hours.

$$\text{Bacteria at the end of 2 hours} = P \left(1 + \frac{R}{100}\right)^n$$

$$= 512000 \times \left(1 + \frac{\frac{5}{2}}{100}\right)^2$$

$$= 512000 \times \left(1 + \frac{1}{40}\right)^2$$

$$= 512000 \times \left(\frac{41}{40}\right)^2$$

$$= 512000 \times \frac{41}{40} \times \frac{41}{40}$$

$$= 537920$$

Hence, the bacteria at the end of 2 hours is 537920